# Statistics Exercises 

Covariance, correlation, the t-test

1. Consider the following data:

| x | 0 | 2 | 4 | 5 | 7 | 8 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y | 4 | 3 | 1 | 1 | 2 | 1 | 0 |

Calculate the correlation coefficient between variables $x$ and $y$.
2. Consider the following data:

| x | 0 | 2 | 4 | 6 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| y | 0 | 1 | 2 | 3 | 4 |

Calculate the correlation coefficient between variables $x$ and $y$. What does this mean?
3. We want to check if on average a cup of butter contains 250 grams or less. A sample test of 25 cups reveals an average of 248.2 grams and a standard deviation of 2.5 grams. Check whether the smaller mean is a significant difference for a significance threshold of $5 \%$.
4. We want to find out if persons of 40 years old are on average heavier than persons of 30 years old. We have taken two independent sample sets, given as follows:

| 30y weight | 77 | 65 | 73 | 58 | 63 | 49 | 51 | 82 | 103 | 69 |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 40y weight | 102 | 73 | 56 | 55 | 83 | 72 | 88 | 70 | 81 | 85 | 44 | 71 | 62 | 78 | 75 |

Give an analysis of this situation and use the t-test to find out whether our hypothesis is valid for a significance threshold of $10 \%$.
5. We want to check if a marketing strategy for playing on-line games has worked. For 8 subjects, we have measured the number of hours they spend per week on on-line games before and after the marketing strategy. This data is given as follows:

| hours played before | 2 | 3 | 1 | 4 | 6 | 2 | 12 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| hours played after | 3 | 2 | 0 | 4 | 7 | 4 | 10 | 10 |

Find out whether the marketing strategy works with a significance threshold of $5 \%$.

